

Finite-Trace Analysis of Stochastic Systems with Silent Transitions

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Teaching and Research
Area of Business Process
Management, Foundations
and Engineering

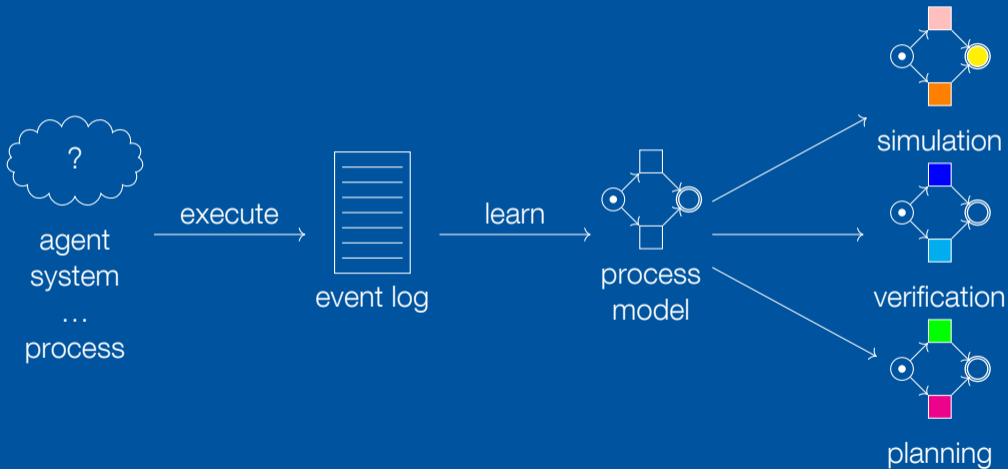
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Systems



system

Process Mining

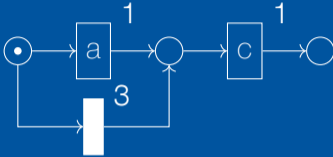


Event logs

$$L_1 = [\langle \text{register, check, accept} \rangle^{10000}, \\ \langle \text{register, check, reject} \rangle^{10000}, \\ \langle \text{register, accept} \rangle^1, \\ \langle \text{accept, register} \rangle^1]$$

$$L_2 = [\langle \text{register, check, accept} \rangle^{9500}, \\ \langle \text{register, check, reject} \rangle^{9500}, \\ \langle \text{register, accept} \rangle^{1002}]$$

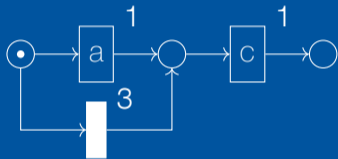
Stochastic Petri nets



Stochastic language:

$$[\langle a, c \rangle^{0.25} \\ \langle c \rangle^{0.75}]$$

The probability problem

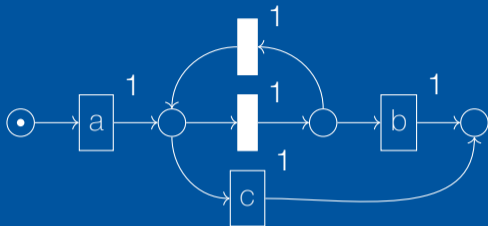


Specification
LTLf

...

When the Petri net produces a trace, what is the probability that this trace adheres to the specification?

An example



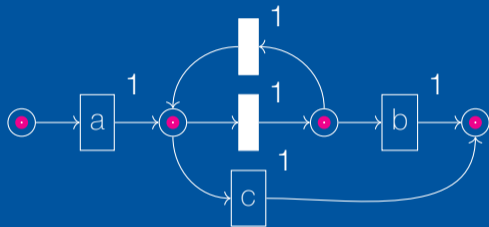
Sum of all paths satisfying the specification.

There are infinitely many such paths...

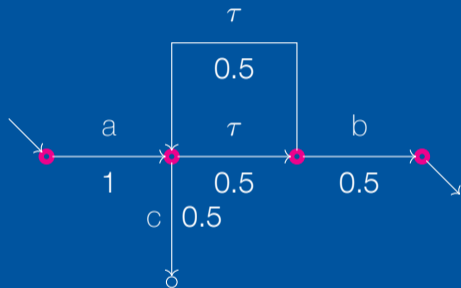


$\langle a, b \rangle$

Solving the probability problem



► Stochastic product automaton



► What is the probability that we end up in the target state?

Standard Markov chain analysis ($\frac{1}{3}$)

You have been watching...

- ▶ Process mining
- ▶ Stochastic Petri nets
- ▶ The probability problem

Future work

- ▶ Stochastic model checkers
- ▶ Exact answers

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